

Epistemology

Lecture 6: Knowledge Analysis – Nozick's Truth-Tracking Account

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Special Topic:
Counterfactuals and Possible Worlds

Indicative conditionals

- These are the most commonly used conditionals in natural language, expressed in the indicative mood.
- Simple Form:
'If P , then Q ' where P and Q are declarative sentences.

NB: Being declarative, such sentences have a truth-value.

Examples:

- * If the UK leaves the EU under the current plan, the UK's GDP will shrink by 3.5% in the next 10 years.
- * If Shakespeare didn't write Hamlet, someone else did.
- * If John isn't helping us, James will gladly do so.

Truth-conditional semantics

- How are we meant to understand the meaning of these conditionals?
- An influential approach is to use truth-conditions:
Meaning equals (or reduces to) truth-conditions.

Example (non-conditional):

‘There are exactly eight planets in the solar system’.



To understand its meaning we need only specify its truth-conditions, viz. it comes out true if and only if there are only eight things that qualify as what we call ‘planets’ in what we call the ‘solar system’.

NB: Other approaches to semantics include the proof-theoretic one.

Semantics for indicative conditionals

- Following this approach to semantics, we specify the meaning of a complex sentence through the truth-conditions of its parts.
- Indicative conditionals are complex sentences. The following truth-table provides the standard way of specifying their truth conditions.
- 'A \rightarrow B' is true if and only if A is false or B is true.
- This conception of indicative conditionals is known as the '**material** conditional / implication'.
- Other conceptions give a different truth-table, e.g. rows 3 & 4 may come out as indeterminate.

	<i>A</i>	<i>B</i>	<i>A \supset B</i>
1.	T	T	T
2.	T	F	F
3.	F	T	T
4.	F	F	T

Subjunctive conditionals

- Forms:

‘If *A* **were (not)** the case, *B* **would (not) be** the case’.

‘If *A* **had (not) been** the case, *B* **would (not) have been** the case’

NB: The antecedent asserts something that we assume to be false. No wonder that such conditionals are a.k.a. ‘**counterfactuals**’.

- Subjunctive conditionals are used to express modal claims.

Examples:

If Jane were not ten minutes late, she would have caught the train.

If Hitler were a pacifist, WWII wouldn’t have happened.

Indicative vs. subjunctive

- Compare:

(1) If Oswald didn't kill Kennedy, someone else did.

Vs.

(2) If Oswald hadn't killed Kennedy, someone else would have.

- 1 questions whether Oswald killed Kennedy but does not question that he died on 22/11/1963 in (otherwise) exactly those circumstances.
- 2 assumes that Oswald did kill Kennedy but asserts that Kennedy would have at some point been assassinated anyway.

Science and counterfactuals

- Counterfactuals are not just aberrations of everyday language and fiction. They seem to pop-up everywhere, including science.

Examples:

* Had the conditions in the first few moments of the big bang been different, there would not have been any matter in the universe.

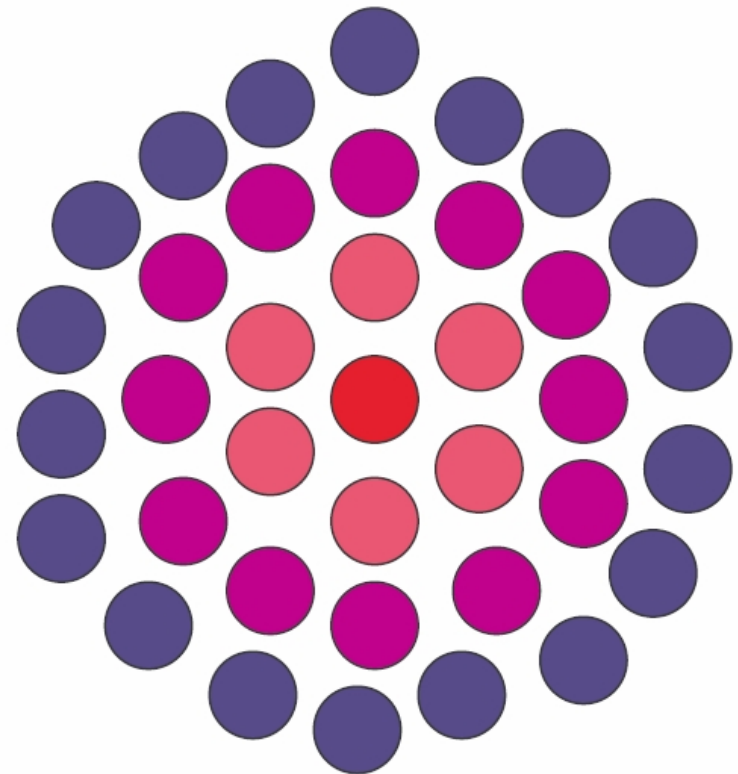
* Were there no forces to act on a body, it would continue at rest or in uniform motion along a straight line.

Semantics for counterfactuals

- The most influential way to understand the truth conditions of counterfactual conditionals is through possible worlds.
- Truth-conditions become relations between possible worlds.
- What's a possible world? It doesn't have to be a real world as David Lewis holds. Rather, it can be merely a device to express modal claims.
- For any way the actual world could have been (but isn't) we **imagine** another world instantiating those differences.
- These are the possible non-actual worlds. Note that the actual world is also possible!

Possible world semantics

- **Proposal:** The counterfactual ‘If X were the case, then Y would be the case’ (formally: ‘ $X \Box \rightarrow Y$ ’) holds or is true *if and only if* Y holds in all X -worlds which are closest to the actual world.
- Colour-coding scheme:
 - Red:** The actual world
 - Pink:** Closest possible worlds
 - Violet:** Worlds not close enough
 - Purple:** Furthest possible worlds
- The closest the world, the more similar to the actual world. Such worlds are meant to differ only by one small fact (and any knock-on differences that change demands).



Chapter I: Nozick's Theory

The sensitivity-to-truth connection

- Recall from the last two lectures that truth and belief need to connect in the right way.
- One proposal for how to achieve this is through ‘truth-tracking’ across close possible worlds.
- That is, belief in a given proposition must be sensitive to the truth by checking what happens in nearby possible worlds.
- **Hint:** If something is luckily believed (in the actual world), then we imagine that in nearby worlds it is not believed.

Nozick's truth-tracking theory

- S knows that p if and only if

(i) S **believes** that p ,

(ii) p is **true**,

(iii) If p were not true, S wouldn't believe p .

(iv) If p were true, S would believe p .

NB1: Nozick (1981) actually goes for a variant of the above that incorporates reference to a *method* through which S knows p .

NB2: See also Dretske (1970; 1971; 1972; 2005).

- As we will soon see, counterfactual conditions iii and iv are there to combat cases where truth and belief line up accidentally.

The third condition

- Let us consider the third condition in more detail:
(iii) If p were not true, S wouldn't believe p .
- Suppose p is true by accident in the actual world. Presumably, in the closest worlds p is false - and (almost) everything else is the same
- Does S still believe p in those worlds?
- If YES, then S doesn't know p . That is, if S is consistently wrong like that across close possible worlds, S doesn't know p .

NB: Condition (ii) is still satisfied as in the actual world p is true.

The Smith-Jones case revisited

- Smith **believes** that the person who gets the job has ten coins in their pocket. So, **condition (i) is satisfied**. The proposition ‘The person who gets the job...’ is **true**. So, **condition (ii) is satisfied**.

In the closest possible world(s), the accident of Smith having 10 coins in his pocket doesn’t happen. That means p is false in those worlds.

Presumably, **in such world(s) Smith would still believe p** – recall the ceteris paribus clause. So, **condition (iii) is NOT satisfied!**

Thus, Smith doesn’t know p . This verdict accords with the intuitions Gettier seems to be eliciting in that counterexample.

The dog in sheep's clothing revisited

- ***S* believes** that there is a sheep in the prairie. So, **condition (i) is satisfied**. The proposition 'There is a sheep in the prairie' is **true**. So, **condition (ii) is satisfied**.
- In the closest possible world(s), the accident of the real sheep being in the prairie doesn't happen. That is, p is not true in those worlds.
- But, presumably, in such world(s) ***S* would still believe p** – recall the ceteris paribus clause. So, **condition (iii) is NOT satisfied!**
- **Thus, *S* doesn't know p** . Again, this accords with the standard intuitions!





Does Henry (of fake barn land repute) know according to Nozick's theory?

Yes

No

The fake barns case revisited

- Henry **believes** that there is a real barn in an area. So, **condition (i) is satisfied**. The proposition 'There is a real barn in this area' is **true**. So, **condition (ii) is satisfied**.

In the closest possible world(s), the barn Henry is looking at is fake. That is, p is not true in those worlds. Presumably, in such world(s) **Henry would still believe p** . So, **condition (iii) is NOT satisfied!**



- Thus, Henry doesn't know p** as per the intuitions of those who put forth this case.

Counterexample: Kripke's barns

- Henry **believes** that there is a red barn in an area. So, **condition (i) is satisfied**. The proposition p : 'There is a red barn in this area' is **true**. So, **condition (ii) is satisfied**.

In the closest world(s), the barn is not red, e.g. it is yellow, but not fake. That is, p is not true in those worlds.

Presumably in such world(s), **Henry would not believe p** . **Condition (iii) is thus satisfied!**

- **Thus**, (provided condition iv is also satisfied) **Henry knows that p** .

Counterexample: Kripke's barns (2)

- Because Henry believes there is a red barn, he also **believes** that there is a barn in this area, i.e. **condition (i) is satisfied**. The proposition p' : 'There is a barn in this area' is **true**. So, **condition (ii) is satisfied**.

In the closest world(s) the barn is fake, i.e. p' is false in those worlds. But **Henry still believes p'** . So, **condition (iii) is NOT satisfied!**

Thus, Henry doesn't know p' . That's regardless of whether condition iv is satisfied as condition iii is not satisfied.

That seems **absurd**. According to Nozick's account, Henry knows that there is a red barn, i.e. p , but he doesn't know that there is a barn, p' .

The fourth condition

- Let us consider the fourth condition in more detail:

(iv) If p were true, S would believe p .

- Suppose p is true in the closest possible worlds but some other minor things are different.

NB: I can't stress the importance of the latter, i.e. the other minor things being different, enough!!!

- If S would still believe p in those worlds, i.e. if they consistently tracking the truth like that, then we say that S knows p .

The clock case revisited



- ***S* believes** that it is 8:21. So, **condition (i) is satisfied**. The proposition 'The time is 8:21' is **true**. **Condition (ii) is satisfied**.

Take the closest possible world(s) where p is true, i.e. it is 8:21. Suppose the clock in these world(s) stops at different times.

Presumably, in such worlds ***S* would no longer believe p** . So, **condition (iv) is NOT satisfied!**

Thus, *S* doesn't know p . This accords with the intuitions elicited in that counterexample.





In the same case (i.e. the clock case), is condition (iii) satisfied? Why? Why not?

The End